

1. Weekly sales for a grocery store follow a normal distribution with mean 300,000 and standard deviation 25,000. Use the Empirical Rule to approximate the following probabilities.

- (a) What is the probability the store will have between 250,000 and 350,000 in sales next week?

Answer:

This is the area within 2 standard deviations of the mean and thus the probability is 95% by the Empirical Rule.

- (b) What is the probability the grocery store will have less than 275,000 in sales next week?

Answer:

This is the area below 1 standard deviation less than the mean. We know that $1 - 0.68 = 0.32$ area is outside of 1 standard deviation and the area below 1 standard deviation is $0.32/2 = 0.16$.

- (c) What is the probability the grocery store will have greater than 375,000 in sales next week?

Answer:

This is the area above 3 standard deviations greater than the mean. We know that $1 - 0.997 = 0.003$ area is outside of 3 standard deviations and the area above 3 standard deviations is $0.003/2 = 0.0015$.

2. The end-of-day inventory at a semiconductor chip storage facility follows a normal distribution with mean 1,500 with a standard deviation of 500. Use the Empirical Rule to approximate the following probabilities.

- (a) What proportion of days have an inventory between 1,000 and 2,000 chips?

Answer:

This is within 1 standard deviation of the mean and thus the probability is 0.68.

- (b) What proportion of days have an inventory above the facilities storage limit of 3,000 chips?

Answer:

This is the area above 3 standard deviations of the mean. We calculated this in 1c) as 0.0015.

- (c) Why might the normal distribution not be a reasonable model for these data?

Answer:

The normal distribution may not be a reasonable model because the number of chips must be positive, but the normal distribution allows negative numbers. In this case, there is only 0.0015 area below 0 and thus this discrepancy will likely not matter too much.